

TRAPPED MODES FOR SPS & LHC COLLIMATOR

E. Métral

- ◆ **Tune shift for the SPS prototype of the LHC collimator (update from the last meeting after discussion with A. Grudiev)**
- ◆ **Multi-bunch tune shifts for the LHC at top energy**

TABLE OF TRANSVERSE MODES FOR FULL GAP = 5 MM (FROM A. GRUDIEV, RLC meeting, 28/01/05)

| f [GHz] | Q | r ₁ /Q [Ohm/mm ²] | r ₁ [Ohm/mm ²] | k ₁ [V/nC/mm ²] | r _t /Q [Ohm/mm] | r _t [Ohm/mm] | k _t [V/nC/mm] | k _t (Py) [V/nC/mm] |
|---------|------|--|---------------------------------------|--|----------------------------|-------------------------|--------------------------|-------------------------------|
| 0.605 | 139 | 6.105e-004 | 8.486e-002 | 5.802e-004 | 4.815e-004 | 6.693e+000 | 4.576e-002 | 4.507e-002 |
| 0.769 | 612 | 1.467e-006 | 8.976e-004 | 1.772e-006 | 9.12e-005 | 5.570e-002 | 1.099e-004 | 1.078e-004 |
| 0.799 | 639 | 8.823e-007 | 5.638e-004 | 1.107e-006 | 1.12e-005 | 3.367e-002 | 6.613e-005 | 6.769e-005 |
| 0.848 | 687 | 1.135e-005 | 7.798e-004 | 1.107e-006 | 1.12e-005 | 4.388e-001 | 8.508e-004 | 8.432e-004 |
| 0.909 | 751 | 1.449e-005 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 5.710e-001 | 1.086e-003 | 1.074e-003 |
| 1.226 | 934 | 4.174e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 1.517e+002 | 3.128e-001 | 3.154e-001 |
| 1.228 | 961 | 9.441e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 3.525e+002 | 7.076e-001 | 7.040e-001 |
| 1.255 | 1070 | 1.473e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 5.993e-001 | 1.104e-003 | 1.072e-003 |
| 1.295 | 808 | 6.198e-003 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 1.845e+002 | 4.645e-001 | 4.513e-001 |
| 1.306 | 570 | 9.626e-005 | 5.487e-003 | 2.917e-005 | 5.282e-004 | 2.005e+000 | 7.214e-003 | 6.707e-003 |
| 1.312 | 560 | 1.452e-005 | 8.134e-003 | 2.917e-005 | 5.282e-004 | 2.958e-001 | 1.089e-003 | 1.178e-003 |
| 1.315 | 530 | 1.910e-005 | 1.012e-002 | 3.486e-006 | 6.929e-004 | 3.672e-001 | 1.431e-003 | 1.255e-003 |
| 1.565 | 1294 | 1.143e-007 | 1.480e-004 | 1.107e-006 | 1.12e-005 | 4.511e-003 | 8.570e-006 | 9.109e-006 |
| 1.595 | 172 | 1.158e-002 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 5.957e+001 | 8.677e-001 | 8.508e-001 |
| 1.611 | 171 | 1.288e-005 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 3.817e-004 | 6.526e-002 | 9.656e-004 |
| 1.636 | 170 | 8.031e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 3.982e+002 | 6.019e+000 | 5.867e+000 |
| 1.659 | 925 | 1.585e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 4.216e-006 | 1.188e-008 | 1.182e-008 |
| 1.672 | 169 | 5.281e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 2.541e+002 | 3.949e+000 | 3.924e+000 |
| 1.673 | 940 | 9.211e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 2.478e-003 | 6.927e-006 | 6.866e-006 |
| 1.674 | 1356 | 2.811e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 1.085e-002 | 2.103e-005 | 2.075e-005 |
| 1.696 | 945 | 2.061e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 5.481e-005 | 1.545e-007 | 1.470e-007 |
| 1.717 | 168 | 2.603e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 1.215e+002 | 1.951e+000 | 1.872e+000 |
| 1.727 | 958 | 6.217e-006 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 1.646e-005 | 4.660e-008 | 6.611e-008 |
| 1.767 | 981 | 5.264e-011 | 1.107e-006 | 1.107e-006 | 1.12e-005 | 1.394e-006 | 3.945e-009 | 4.446e-009 |
| 1.772 | 167 | 1.948e-001 | 3.255e-001 | 3.255e-001 | 5.245e+000 | 8.759e+002 | 1.460e+001 | 1.429e+001 |
| 1.785 | 1430 | 9.523e-010 | 1.362e-006 | 2.670e-009 | 2.546e-008 | 3.640e-005 | 7.138e-008 | 1.497e-007 |
| 1.815 | 1012 | 3.334e-008 | 3.374e-005 | 9.506e-008 | 8.765e-007 | 8.870e-004 | 2.499e-006 | 2.525e-006 |
| 1.835 | 165 | 1.318e-001 | 2.175e+001 | 3.800e-001 | 3.428e+000 | 5.656e+002 | 9.881e+000 | 9.742e+000 |
| 1.868 | 1028 | 4.096e-007 | 4.210e-004 | 1.202e-006 | 1.046e-005 | 1.075e-002 | 3.070e-005 | 3.003e-005 |
| 1.898 | 1494 | 3.463e-008 | 5.173e-005 | 1.032e-007 | 8.705e-007 | 1.300e-003 | 2.595e-006 | 2.913e-006 |
| 1.906 | 164 | 2.506e-003 | 4.109e-001 | 7.502e-003 | 6.272e-002 | 1.029e+001 | 1.878e-001 | 1.866e-001 |
| 1.930 | 1067 | 3.838e-007 | 4.095e-004 | 1.164e-006 | 9.489e-006 | 1.012e-002 | 2.877e-005 | 2.992e-005 |
| 1.983 | 164 | 7.304e-002 | 1.198e+001 | 2.275e-001 | 1.757e+000 | 2.882e+002 | 5.474e+000 | 5.509e+000 |
| 1.995 | 1000 | 8.990e-006 | 8.990e-003 | 2.817e-005 | 2.150e-004 | 2.150e-001 | 6.738e-004 | 7.114e-004 |

**Linac's convention
⇒ Divide by 2 for rings**

**Can be obtained
from the loss factor :**

$$R_t = \frac{Q k_t}{\pi f} \left(= \frac{r_t}{2} \right)$$

⇒ The results of last week should be divided by 2

SPS HORIZONTAL SINGLE-BUNCH TUNE SHIFT FOR THE HEAD-TAIL MODE $M = 0$

TM1 : -2.03983×10^{-9}
TM2 : -5.81091×10^{-9}
TM3 : -1.3119×10^{-8}
TM4 : -8.08981×10^{-9}
TM5 : -1.24454×10^{-10}
TM6 : -1.1967×10^{-8}
TM7 : -8.07584×10^{-8}
TM8 : -5.1747×10^{-8}
TM9 : -2.484×10^{-8}
TM10 : -1.79741×10^{-7}
TM11 : -1.17202×10^{-7}
TM12 : -2.14036×10^{-9}
TM13 : -5.98159×10^{-8}

With the experimental
parameters ($E = 270 \text{ GeV} \dots$)
 \Rightarrow See FZ's talk at LCE
meeting (22/10/04)

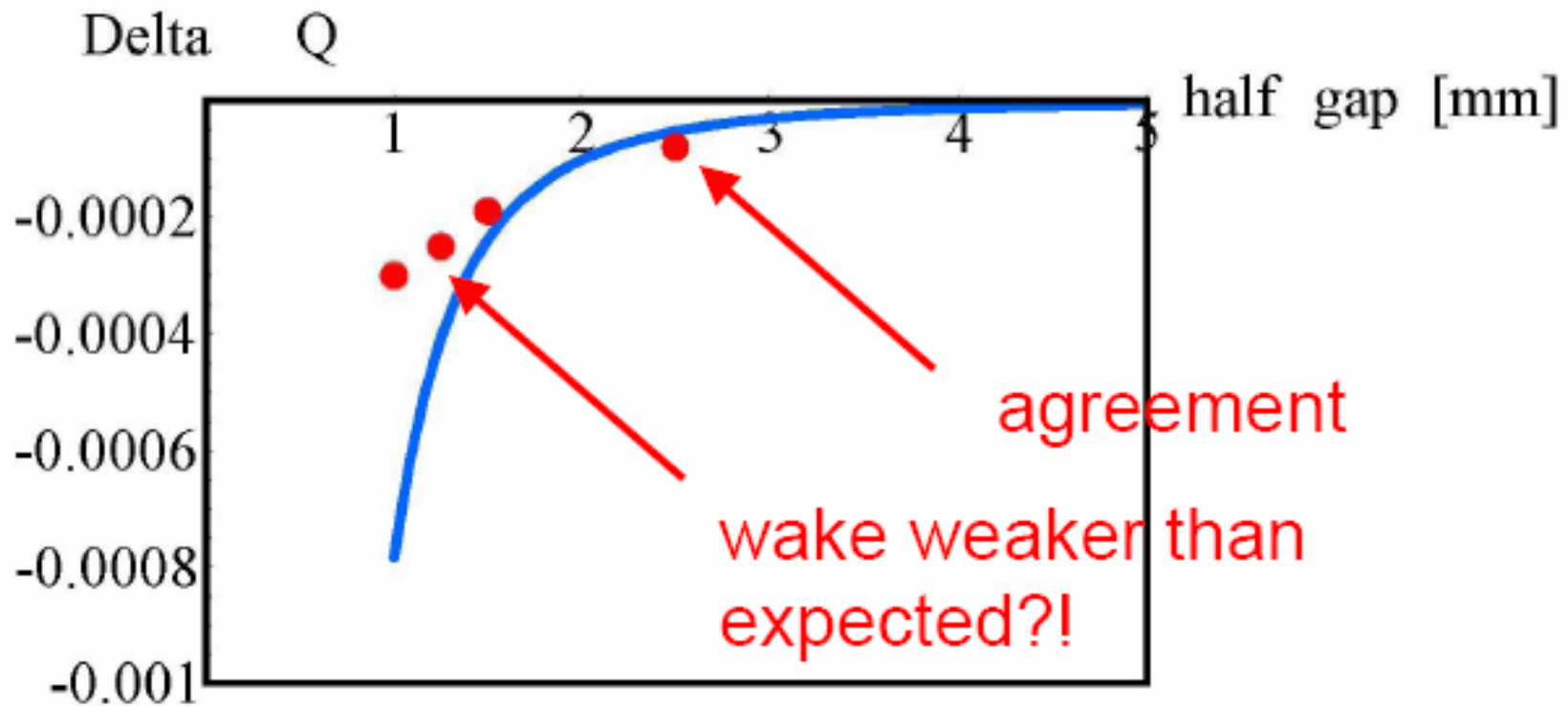
$$\text{Im}[Z_{x,m=0}^{eff, \text{All TMs}}] \approx 4.6 \text{ k}\Omega/\text{m}$$

$$\Delta Q_{x,m=0}^{\text{SB, All TMs}} \approx -5.6 \times 10^{-7}$$

\Rightarrow Seems negligible compared to
the measured tune shift of $\sim 10^{-4}$

FZ'S RESULT

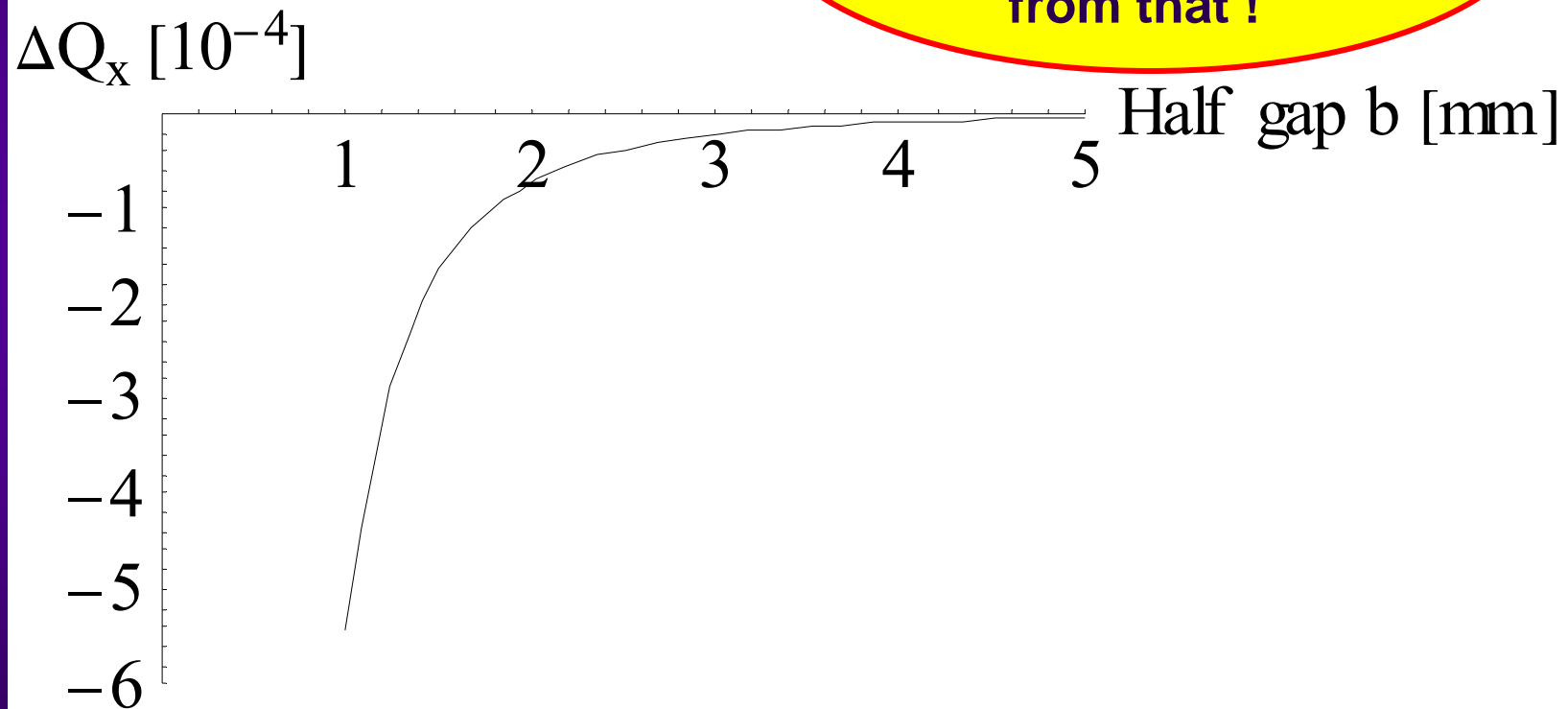
comparison of measured & predicted ΔQ



Expected tune shift of a pencil beam of constant intensity of 8.5×10^{10} protons, on which the measured data (from Marek Glasier's APC talk) are superimposed.

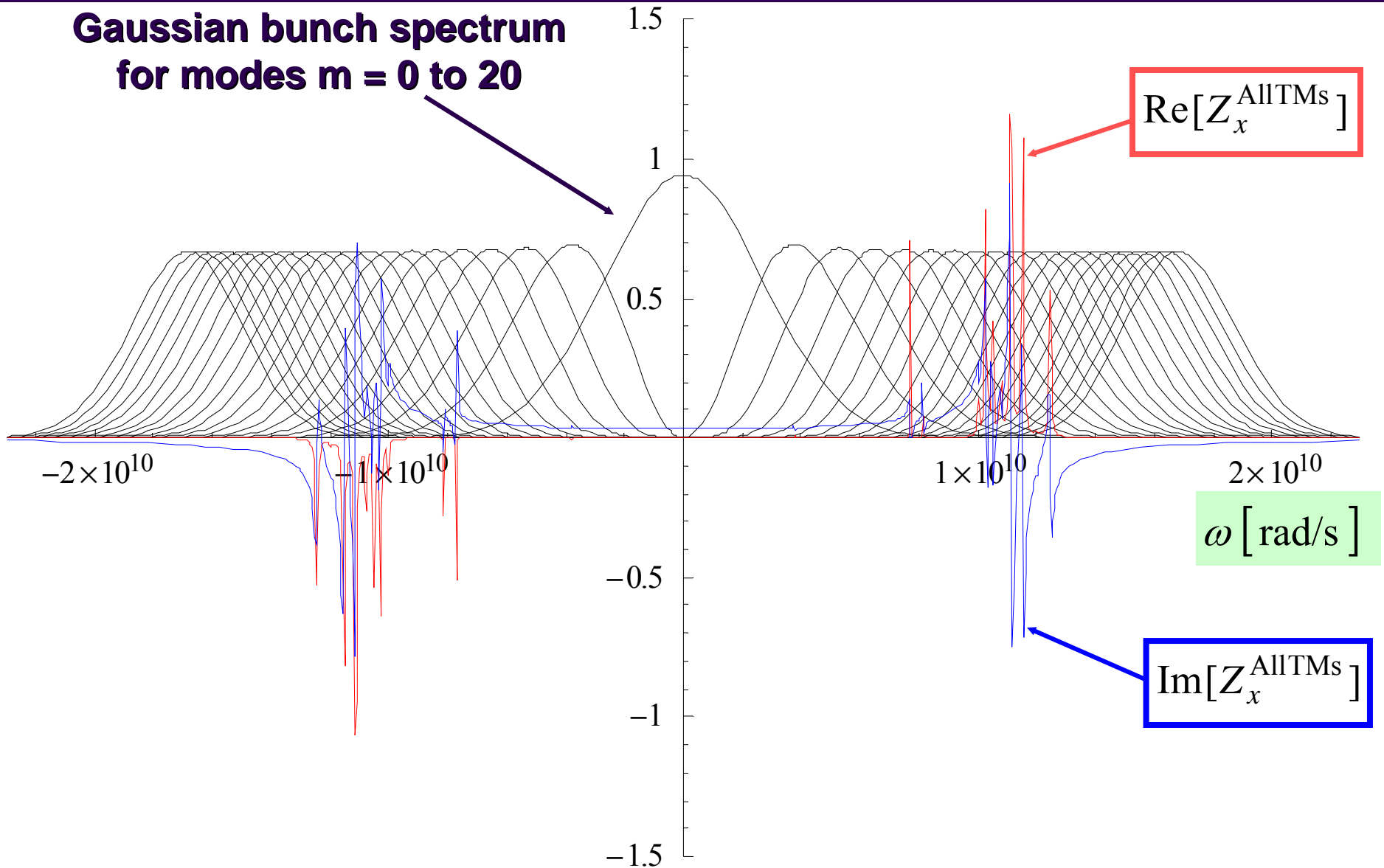
**THE RESULT I OBTAINED
(USING THE SAME PARAMETERS ... BUT THE MEASUREMENT
PARAMETERS HAVE TO BE CONFIRMED FOR EACH GAP !)**

**May be part of the
difference between theory
and measurements come
from that !**



MULTI-BUNCH TUNE SHIFTS FOR THE LHC AT TOP ENERGY (1/5)

Gaussian bunch spectrum
for modes $m = 0$ to 20



MULTI-BUNCH TUNE SHIFTS FOR THE LHC AT TOP ENERGY (2/5)

For 1 collimator with most critical betatron function (~ 400 m)

$$-7.35496 \times 10^{-7} - 8.30054 \times 10^{-9} \text{ i}$$

$$-4.52494 \times 10^{-7} - 3.55758 \times 10^{-8} \text{ i}$$

$$-3.866 \times 10^{-7} - 6.81186 \times 10^{-8} \text{ i}$$

$$-3.64841 \times 10^{-7} - 8.94599 \times 10^{-8} \text{ i}$$

$$-3.42943 \times 10^{-7} - 9.19787 \times 10^{-8} \text{ i}$$

$$-3.03872 \times 10^{-7} - 7.97902 \times 10^{-8} \text{ i}$$

$$-2.43904 \times 10^{-7} - 6.15077 \times 10^{-8} \text{ i}$$

$$-1.68694 \times 10^{-7} - 4.73627 \times 10^{-8} \text{ i}$$

$$-8.96369 \times 10^{-8} - 4.09279 \times 10^{-8} \text{ i}$$

$$3.51564 \times 10^{-8} - 3.20641 \times 10^{-8} \text{ i}$$

$$7.30457 \times 10^{-8} - 2.32251 \times 10^{-8} \text{ i}$$

$$9.40848 \times 10^{-8} - 1.5836 \times 10^{-8} \text{ i}$$

$$1.00594 \times 10^{-7} - 1.03212 \times 10^{-8} \text{ i}$$

$$9.67417 \times 10^{-8} - 6.50222 \times 10^{-9} \text{ i}$$

$$8.69313 \times 10^{-8} - 3.98337 \times 10^{-9} \text{ i}$$

$$7.47613 \times 10^{-8} - 2.37543 \times 10^{-9} \text{ i}$$

$$6.26328 \times 10^{-8} - 1.37523 \times 10^{-9} \text{ i}$$

$$5.18309 \times 10^{-8} - 7.69482 \times 10^{-10} \text{ i}$$

$$4.28261 \times 10^{-8} - 4.14216 \times 10^{-10} \text{ i}$$

$$3.56027 \times 10^{-8} - 2.13771 \times 10^{-10} \text{ i}$$

$$2.99192 \times 10^{-8} - 1.05562 \times 10^{-10} \text{ i}$$

MULTI-BUNCH TUNE SHIFTS FOR THE LHC AT TOP ENERGY (3/5)

⇒ Instability rise-time for the most critical mode ($m = 4$) : ~ 155 s

REMINDER

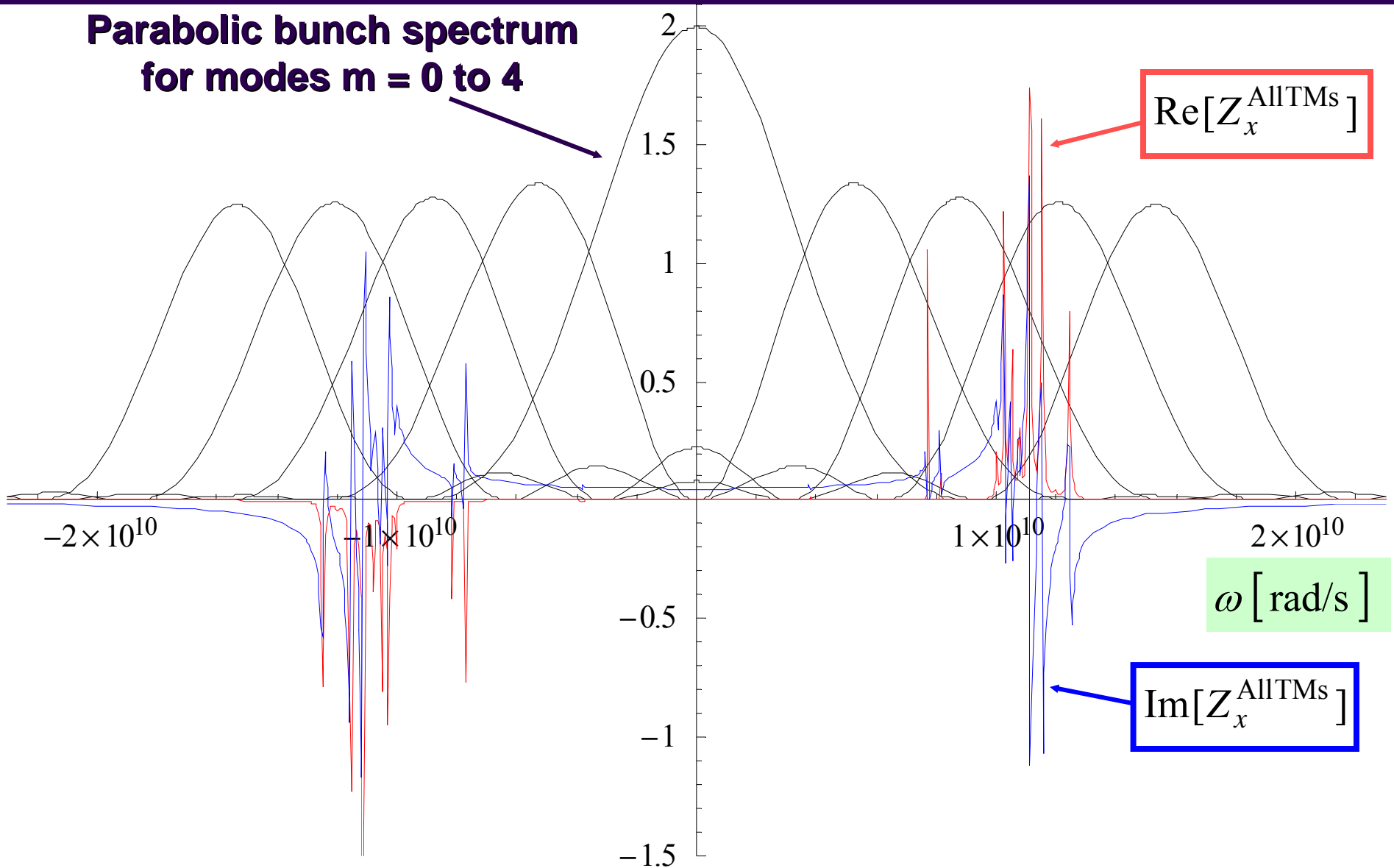
Present baseline for Phase 1

- IR7 : 3 P + 11 S = 14 collimators
- IR3 : 1 P + 4 S = 5 collimators

⇒ 19 collimators in total = 4 P + 15 S

MULTI-BUNCH TUNE SHIFTS FOR THE LHC AT TOP ENERGY (4/5)

Parabolic bunch spectrum
for modes $m = 0$ to 4



MULTI-BUNCH TUNE SHIFTS FOR THE LHC AT TOP ENERGY (5/5)

For 1 collimator with most critical betatron function (~ 400 m)

$$-7.39047 \times 10^{-7} - 1.08558 \times 10^{-8} i$$

$$-5.91127 \times 10^{-7} - 1.07342 \times 10^{-7} i$$

$$-4.9059 \times 10^{-7} - 1.28585 \times 10^{-7} i$$

$$1.47576 \times 10^{-7} - 5.53814 \times 10^{-8} i$$

$$1.75721 \times 10^{-7} - 4.18932 \times 10^{-9} i$$

\Rightarrow Instability rise-time for the most critical mode ($m = 2$): ~ 110 s