

# update on SPS impedance localization

two outstanding actions

(APC 26/05/2005, reminder GA 29.01.06):

- the available information on the transverse impedance from rf cavities (or others?) should be included in the model
- explore possibility that the impedance source in Sextant 5 is compatible with a localized source in 517 (instrumentation - IPM in particular)

(1) include rf 'broadband'  
impedance?

# rf impedance - knowledge

meeting with Elena Shaposhnikova on 02.02.2006,  
providing two papers:

T. Bohl/U. Wehrle, 'RF Installations in the SPS'  
updated 2006-01-25

T.P.R. Linnecar, E.N. Shaposhnikova, 'Resonant  
Impedances in the SPS,' SL-Note 96-49 RF

TW 200 MHz,  $f_r=938.5$  MHz (V),  $R/Q=16.4 \Omega$ ,  
 $Q=1500$ ,  $Z_{total}=2.49$  M $\Omega$ /m, 4 cavities, at  
locations 2832.32 m, 2866.35 m, 2897.95 m,  
2928.62 m

TW 800 MHz,  $f_r=1146$  MHz,  $R/Q=335 \Omega$ ,  $Q=1000$ ,  
 $Z_{total}=4.0$  M $\Omega$ /m, 2 cavities at locations 2843.80  
m, 2854.87 m

Form of the transverse resonator impedance:

RF Group seems to use following formula for the transverse broadband impedance:

$$Z_{\perp} = \frac{\omega}{c} \frac{R_s}{1 + iQ \left( \frac{\omega_R}{\omega} - \frac{\omega}{\omega_R} \right)}$$

where  $R_s$  is in units of  $\Omega$

Alex Chao's textbook:

$$Z_{\perp} = \frac{\omega_R}{\omega} \frac{Z_t}{1 + iQ \left( \frac{\omega_R}{\omega} - \frac{\omega}{\omega_R} \right)} = \frac{c}{\omega} \frac{R_s}{1 + iQ \left( \frac{\omega_R}{\omega} - \frac{\omega}{\omega_R} \right)}$$

where  $R_s$  is in units of  $\Omega/\text{m}^2$

SL Note 96-49 RF:

$$Z_{\perp} = \frac{R_{\perp}}{Q} Q \frac{L}{4} \frac{2\pi f_{rf}}{c}$$

travelling wave cavity

$$Z_{\perp} = \frac{R_{\perp}}{Q} Q \frac{2\pi f_{rf}}{c}$$

standing wave cavity

if I use these last relations which is the functional form of the impedance?

tentatively I now take transverse impedance  $Z_t$  from SL note, but then I identify it with  $Z_t$  in the expression derived from Alex' textbook, and employ this latter formula for computing an effective impedance

doing so I obtain:

$$Z_{eff} \sim -i 1685 \Omega/m \text{ for 200-MHz system}$$

$$Z_{eff} \sim -i 4040 \Omega/m \text{ for 800-MHz system}$$

these numbers are much smaller than total SPS transverse system  $Z_{eff} \sim -i 20 \text{ M}\Omega/m$

lowest mode is not sufficient to estimate effective impedance for a single bunch

# summary rf impedance

two problems:

- (1) do not have any reasonable estimate for the broadband impedance, only data for 1 HOM
- (2) formula for transverse HOMs does not seem to comply with standard theory (Chao, Ruggiero,...)

I cannot pursue this action further until these problems are resolved

(2) repeat previous analysis using different weights etc., in particular w.r.t. impedance of sector 5

normalize data differently to allow for direct comparison with result of coherent tune shift measurement

current-dependent quadrupole strength is converted into effective impedance:

$$\frac{1}{\sqrt{\pi}} \frac{\sigma_z}{c} \int_{-\infty}^{\infty} \text{Im} Z_{\perp}(\omega) \exp\left(-\frac{\omega^2 \sigma_z^2}{c^2}\right) d\omega = -\frac{\beta}{\langle\beta\rangle} \frac{2\pi\gamma}{r_p} \frac{Z_0 c}{4\pi} \left[\frac{\Delta K}{\Delta N}\right] \frac{1}{\sqrt{\pi}} \frac{\sigma_z}{c}$$

||

$$\text{Im} Z_{\perp,eff} \approx 3.2 \times 10^{20} \Omega \frac{\Delta K}{\Delta N} \quad \text{for 14 GeV/c} \\ \text{\& } \sigma_z = 0.3 \text{ m}$$



# potential impedance locations:

MKQ: 1165-1167

MKD: 1173-1175

MKP: 11931-11955

MKE: 41631-41654

RF: 31637-31934

IPM: 4169?

instrumentation: 517

...

# all quadrupoles

initial weight=1, SVD cutoff=5,  $\lambda=10$

fit quality:  $((\Delta\phi/\Delta N)_{\text{fit}} - (\Delta\phi/\Delta N)_{\text{meas}})_{r,s} = 0.00234 (2\pi/10^{11})$

rms impedance strength:  $4.86 \times 10^{-5} [\text{m}^{-1}/10^{11}]$

total impedance  $\Sigma \beta / \langle \beta \rangle \text{Im}(Z) = 30.9 \text{ M}\Omega/\text{m}$

QDA11910 3.05 M $\Omega$ /m

QD63510 1.97 M $\Omega$ /m

QD30110 1.82 M $\Omega$ /m

QD42110 1.75 M $\Omega$ /m

QD50710 1.75 M $\Omega$ /m

QDA41710 1.45 M $\Omega$ /m

QD50110 1.15 M $\Omega$ /m

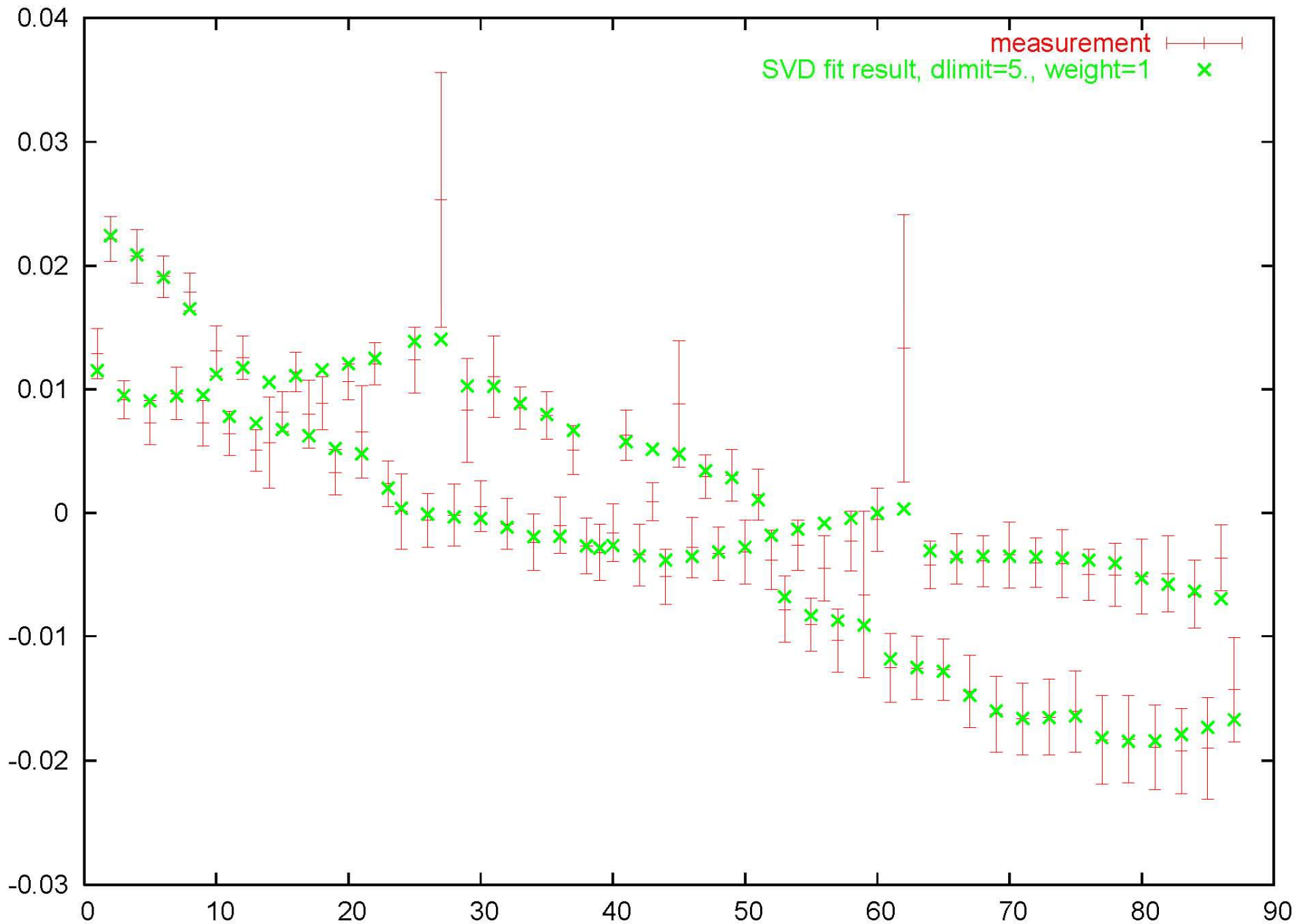
QD10510 1.11 M $\Omega$ /m

QD11510 0.89 M $\Omega$ /m

QD13310 0.83 M $\Omega$ /m

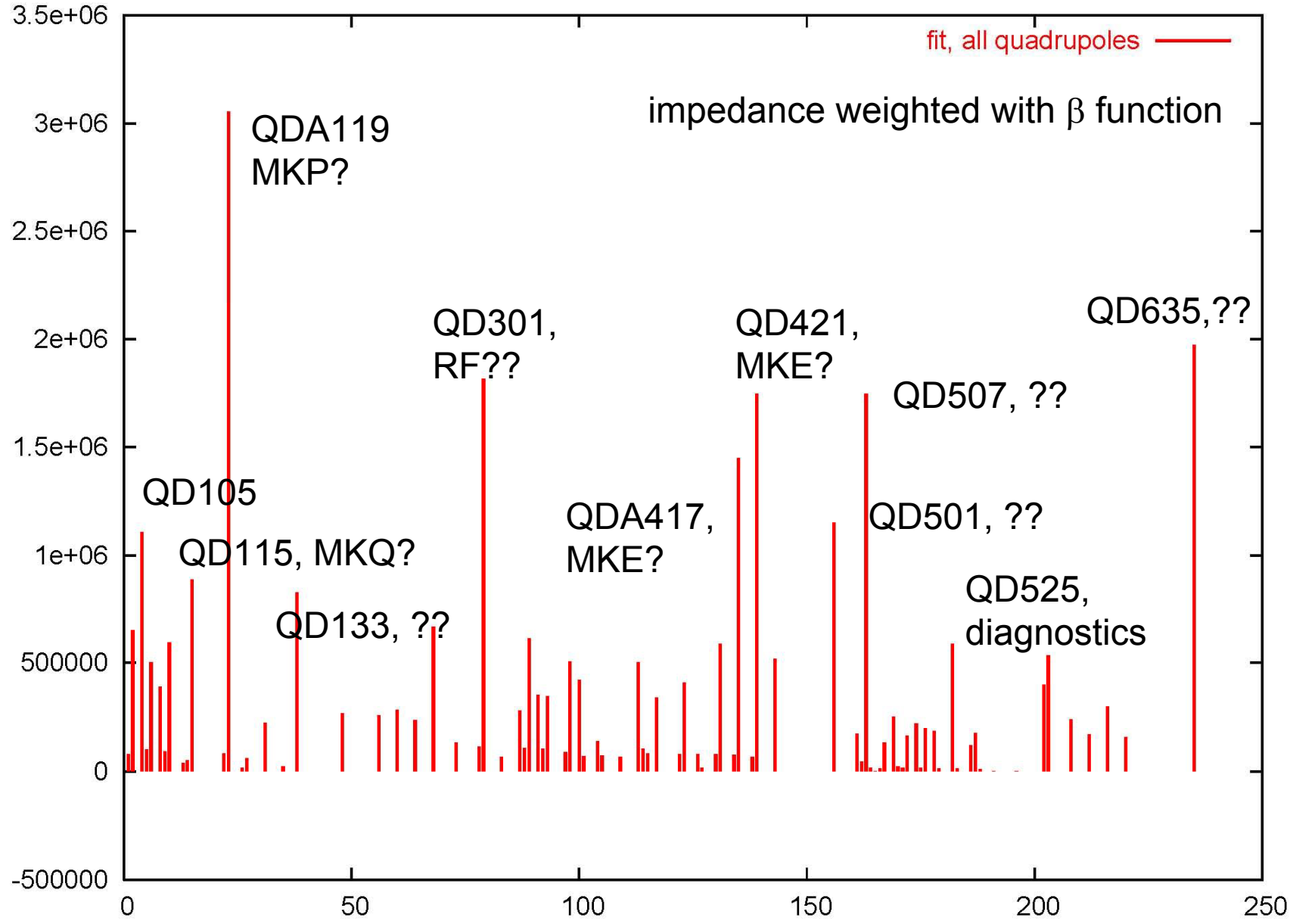
...

# fit with all quadrupoles



$\text{Im}Z_{\text{eff}}$   
[ $\Omega/\text{m}$ ]

fit with all quadrupoles



# without 11 quadrupoles

(w/o QD301, QF300, QD305, QD309, QE302,  
QF308, QD313, QF304, QECD306, QD501, QD507),  
initial weight=1, SVD cutoff=5,  $\lambda=10$

fit quality:  $((\Delta\phi/\Delta N)_{\text{fit}} - (\Delta\phi/\Delta N)_{\text{meas}})_{r,s} = 0.00255 (2\pi/10^{11})$

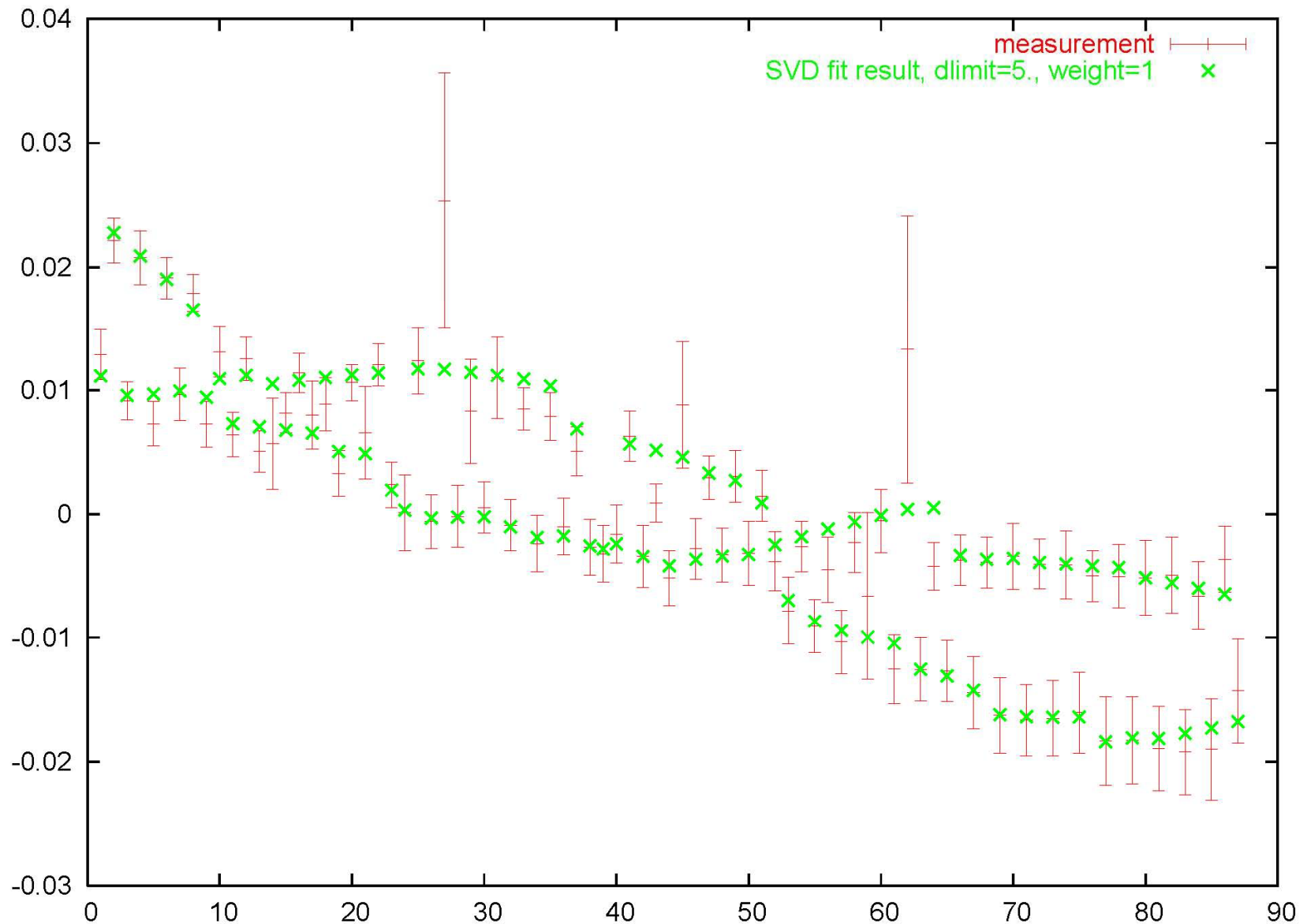
rms impedance strength:  $4.63 \times 10^{-5} [\text{m}^{-1}/10^{11}]$

total impedance  $\Sigma \beta / \langle \beta \rangle \text{Im}(Z) = 29.5 \text{ M}\Omega/\text{m}$

QDA11910	3.24 M $\Omega$ /m
QD42110	1.60 M $\Omega$ /m
QD31710	1.49 M $\Omega$ /m
QD10310	1.49 M $\Omega$ /m
QDA41710	1.46 M $\Omega$ /m
QD11510	1.08 M $\Omega$ /m
QD52510	0.86 M $\Omega$ /m

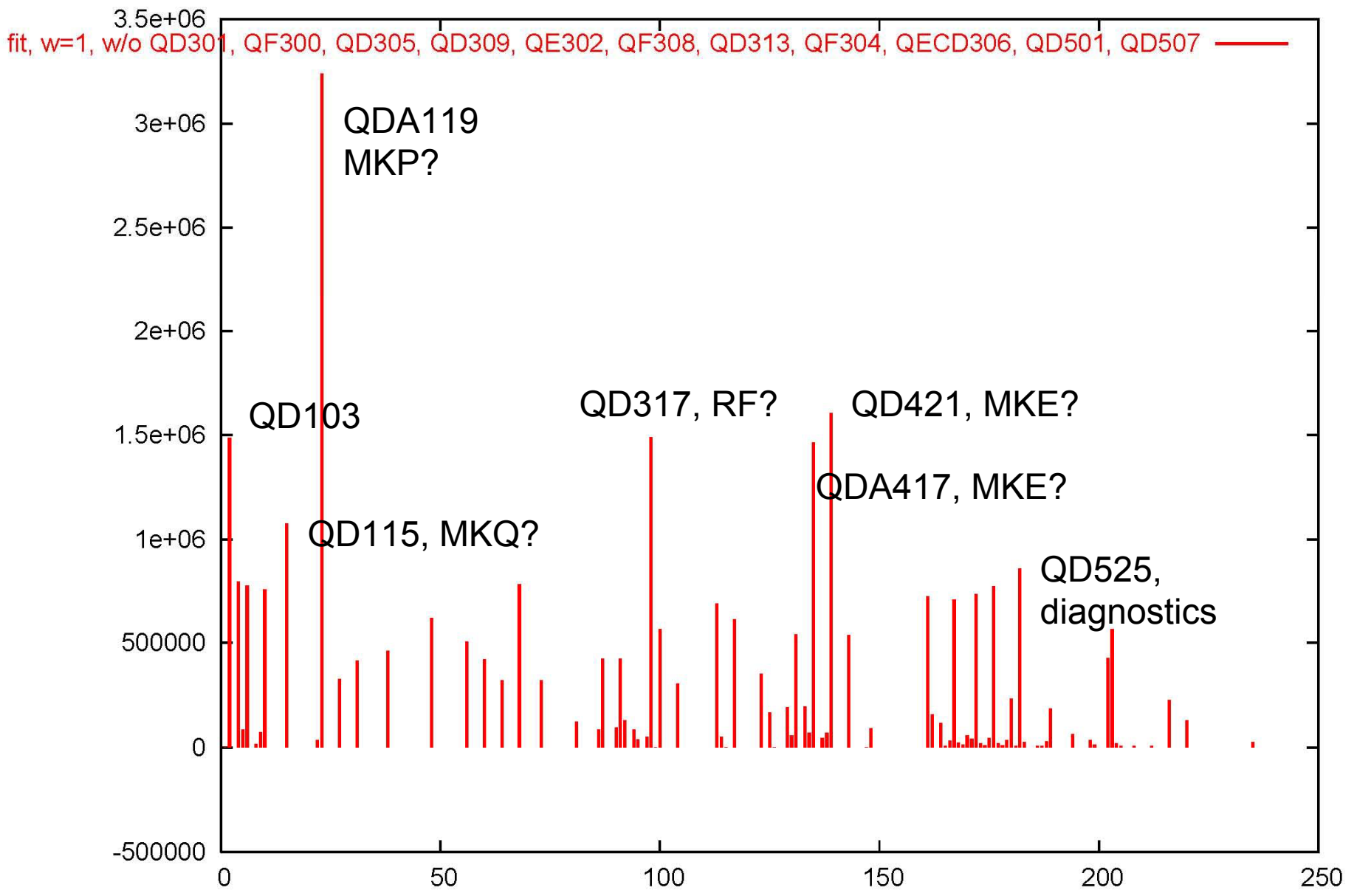
...

fit without 11 quadrupoles: QD301, QF300, QD305, QD309, QE302, QF308, QD313, QF304, QECD306, QD501, QD507



$\text{Im}Z_{\text{eff}}$   
[ $\Omega/\text{m}$ ]

fit without 11 quadrupoles: QD301, QF300, QD305, QD309, QE302, QF308, QD313, QF304, QECD306, QD501, QD507



# another fitting attempt

consider all 'H/V kicker' and 'rf cavity' elements as potential impedance sources instead of the quadrupoles; there are 308 such elements in the SPS MAD model



# with kickers and rf cavities

initial weight=1, SVD cutoff=5,  $\lambda=10$

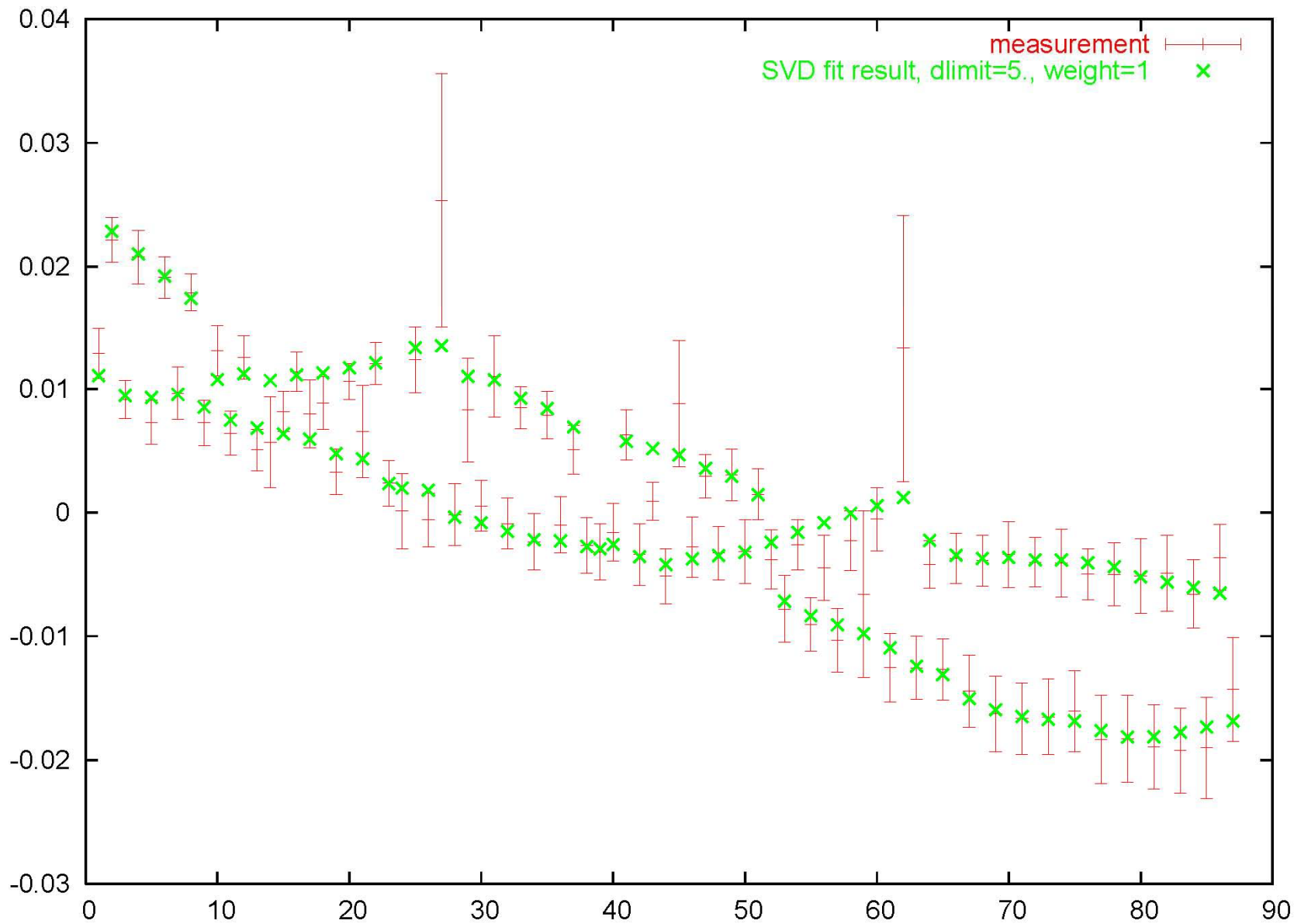
fit quality:  $((\Delta\phi/\Delta N)_{\text{fit}} - (\Delta\phi/\Delta N)_{\text{meas}})_{r,s} = 0.00236 (2\pi/10^{11})$

rms impedance strength:  $3.95 \times 10^{-5} [\text{m}^{-1}/10^{11}]$

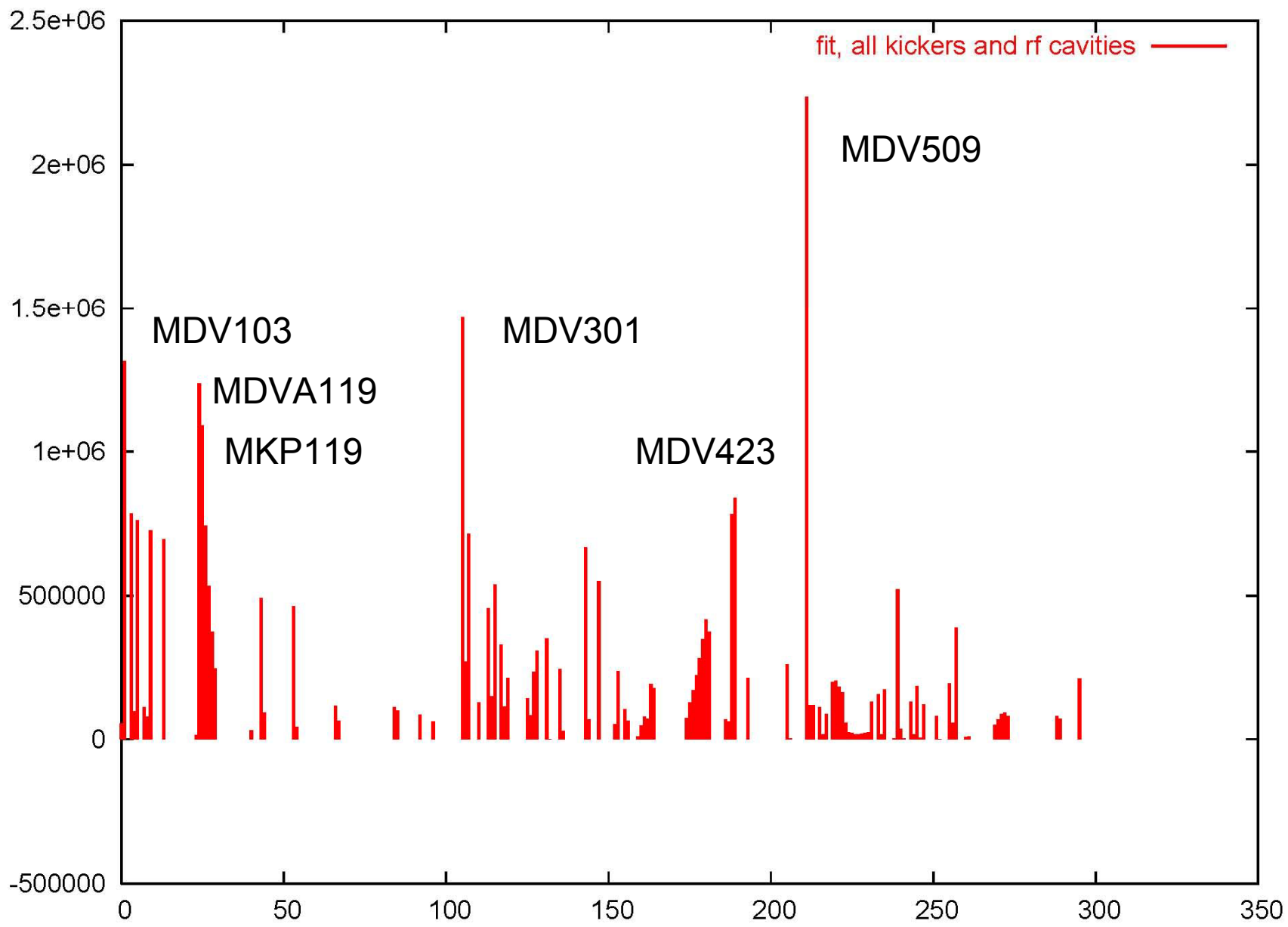
total impedance  $\Sigma \beta / \langle \beta \rangle \text{Im}(Z) = 29.4 \text{ M}\Omega/\text{m}$

MDV50907	2.24 M $\Omega$ /m
MDV30107	1.47 M $\Omega$ /m
MDV10307	1.31 M $\Omega$ /m
MDVA11904	1.24 M $\Omega$ /m
MKP11931	1.09 M $\Omega$ /m
MDV42307	0.84 M $\Omega$ /m

# fit with all kickers and rf cavities (no quadrupoles)



$\text{Im}Z_{\text{eff}}$  fit with all kickers and rf cavities (no quadrupoles)  
[ $\Omega/\text{m}$ ]



# summary of new fitting studies

large impedances are consistently found at the following five locations (both when fitting to quadrupoles and to kickers/rf):

103-105

119 (MKP?)

301 ( $\rightarrow$ 317(RF?) w 9 quads suppressed)

417-423 (MKE?)

501-509 (disappears if quads 501&507  
are removed from the fit)

accurate optics model is essential!